# Study of hydrated Portland cement composition in regard to leaching resistance

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The present paper addresses cement compositions that have an optimal resistance against acid attack and hence, low leaching rates and optimal waste containment. To this end a shrinking core leaching model is used that describes the leaching of metals from a cement sample. This process is directly related to the calcium hydroxide removal from the sample by the acidified leachant. Effective diffusion coefficients in this so-called leached shell were calculated using the equations derived from a cement hydration model. This results in equations in which leaching rates were dependent on cement composition, especially the calcium hydroxide fraction. Optimizing the calcium hydroxide fraction yields cement compositions possessing the optimal leaching resistance as a function of the water porosity. The results were also used for the determination of optimal amounts of silica fume.

Key words: immobilization, shrinking core model, leaching, acid attack, hydration, waste

#### 1. Introduction

Portland cement can be combined with wastes in order to prevent leaching of species such as heavy metals into the environment. This technique is referred to as immobilization or stabilization/ solidification (S/S). The ability of cement with respect to fixing hazardous components and prevention of leaching lies in both physical and chemical properties of the matrix. To test the leaching, cement specimens are subjected to acidified water for prescribed time periods after which metal concentrations in the leachant are measured. In the U.S. the TCLP [U.S. EPA, 1985] and ANS/ANSI 16.1 [ANS, 1986] prescribe the execution of such tests, whereas in The Netherlands recently NEN 7343 [NNI, 1995] and NEN 7345 [NNI, 1995] have been introduced as regulatory tests.

In the past efforts has been made in order to model the leaching from immobilisates and predicting leaching test results. Godbee and Joy (1974) used a semi-infinite medium diffusion model and obtained an expression for the leaching from monoliths. Based on the same bulk diffusion model, Brouwers (1997) derived an expression for the leaching of granular materials. The bulk diffusion model however does not account for the leachant pH nor the observed matrix dissolution taking place in the cement during exposure to an acidic environment (Fattuhi and Hughes, 1988; Cheng, 1991). During this process the portlandite (or Ca(OH)<sub>2</sub>, in cement chemistry notation: CH) present in the cement matrix dissolves. This results in the presence of an unaltered shrinking core and a

moving leached shell in which the CH is removed (Cheng et al., 1991, 1992). Cheng and Bishop (1992) found that in the leached shell stabilized metals were removed while metal concentrations in the core were still unchanged. Hinsenveld (1992) presented a shrinking core model which describes the transport of species by diffusion through this leached shell.

The presence of CH in the cement matrix is of major importance for the leaching. First, this component acts as acid buffer for the acidified water that enters the matrix and releases the contaminants. On the other hand, after dissolution the removed CH generates extra porosity facilitating transport of species by diffusion through the leached shell and resulting in an increasing progress of the dissolution front in the matrix.

Equations for the computation of cement-gel fraction (in cement chemistry notation: CSH), water fraction (or porosity) and CH fractions as function of the water/cement ratio were derived from the cement hydration model developed by Bentz and Garboczi (1991). Furthermore, they simulated CH leaching using their model and derived an expression for the effective diffusion coefficient in a cement matrix during the leaching process (Bentz and Garboczi, 1992; Garboczi and Bentz, 1992). This effective diffusion coefficient mainly depends on the porosity of the matrix, and was in accordance with experimental data (Christensen et al., 1992). Their objective however, was limited to reducing the porosity below the critical value where porosity is not connected anymore. However, the positive effect of the CH phase when it acts as buffering barrier against the acid attack was not considered.

In this paper the results of the mentioned cement hydration model will be used to predict leaching rates as described by the model of Hinsenveld (1992). Combining the analytical expressions yield an optimal composition of hydrated cement and w/c ratio in regard to minimize the leaching rate of the sample. It is believed that this information is of major importance in predicting regulatory test results and creating cement matrices that are effective in containing hazardous contaminants. Subsequently, the analytical predictions are compared with experimental results provided by the literature. Finally, the positive effect of adding silica fume is analyzed in great detail.

## 2 Implementation of matrix composition into leaching model

Following the shrinking core model the cumulative amount leached per unit exposed surface area can be calculated as follows (Hinsenveld and Bishop, 1994; Baker and Bishop, 1997):

$$M(t) = \sqrt{\frac{2 \cdot D_e \cdot C_0^2 \cdot f_{\text{mo}}^2 \cdot C_H}{\beta}} \cdot \sqrt{t}, \tag{1}$$

where:

M(t) = cumulative amount leached contaminant per unit exposed surface area [mol/m<sup>2</sup>],

 $D_a$  = effective diffusion coefficient [m<sup>2</sup>/s],

 $C_0$  = initial metal concentration in sample [mol/m<sup>3</sup>],

 $f_{\text{mo}}$  = mobile fraction of metal,

 $_{CH} = H^{+}$  concentration in leachant [mol/m<sup>3</sup>],

 $\beta$  = acid neutralization capacity (ANC) [mol/m<sup>3</sup>], t = time [s].

As can be seen from equation (1) the release rate depends both on the effective diffusion coefficient of the contaminant species in the leached shell and the acid buffering capacity of the cement specimen.

In the present analysis it is assumed that the acid buffering capacity of cement is directly related to the amount of free calcium present in cement. This calcium originates from both the CH and cement hydrate (in cement chemistry notation: CSH). In a leached shell CH is considered completely dissolved and contributes directly to the ANC, where each mol of CH directly contributes 1 mol of Ca<sup>2+</sup>.

csh also contributes to the ANC, but diffusion of calcium from csh is less complete and much slower than dissolution of Ch (Revertegate et al., 1992; Carde et al., 1996; Faucon et al., 1996; Buil et al., 1992). Revertegate et al. (1992) performed experiments in which immersed opc cement samples (W/C ratio 0.37) were immersed in water at different pH values. After certain periods the samples were analyzed: the total calcium content was determined by XRF, while Ch was analyzed by thermogravimetry. In this way they were able to separate the leaching of calcium from Ch and Csh phases. At pH 4.6, all Ch dissolved and 68 % of the Csh calcium was dissolved. This agrees fairly well with results of Carde et al.(1996) who measured calcium profiles of cement samples with and without Ch after chemical attack by ammonium nitrate. They observed that the Csh phase had a linear decalcification profile from the surface of the sample to the end of the degraded zone, while decalcification of the Ch phase in this zone was complete. For the samples without Ch they found a 50 % decalcification of the Csh in the degraded zone. Considering these experiments an average decalcification value of 0.6 for the Csh will be used in this analysis.

The short-hand notation CSH in fact stands for  $C_{1.7}SH_4$  (Young and Hansen, 1987). This means that 1 mol of CSH can release 1.7 mol  $Ca^{2+}$ . Using the known molar volumes of  $33 \cdot 1(10^3 \, l/mol$  and  $124 \cdot (10^3 \, l/mol$  for CH and CSH, respectively (Young and Hansen, 1987), and the fact that every  $Ca^{2+}$  ion is capable of consuming two  $H^+$ , the equation for the ANC finally takes the following form:

$$\beta = 2 \cdot \frac{\varphi_{\text{CH}}}{33.1 \cdot 10^{-3} \left[\frac{l}{mol}\right]} + 2 \cdot 0.6 \cdot 1.7 \cdot \frac{\varphi_{\text{CSH}}}{124 \cdot 10^{-3} \left[\frac{l}{mol}\right]} = (60.4 \cdot \varphi_{\text{CH}} + 16.5 \varphi_{\text{CSH}}) \left[\frac{l}{mol}\right], \tag{2}$$

where

 $\varphi_{\rm CH}$  = CH volume fraction.

 $\varphi_{\text{\tiny CSH}}$  = CSH volume fraction.

Next, the effective diffusion coefficient of H<sup>+</sup> appearing in equation (1) is related to the porosity of the leached shell. Garboczi and Bentz (1992) derived an equation in which the relative diffusion coefficient of a species in a cement matrix is related to the porosity as follows:

$$\frac{D_{\rm e}}{D_0} = 0.001 + 0.07\,\varphi_{\rm w}^2 + H(\varphi_{\rm w} - 0.18) \cdot 1.8 \cdot (\varphi_{\rm w} - 0.18)^2,\tag{3}$$

where

 $\varphi_w = \text{water porosity},$ 

H(x) = 0 when  $x \le 0$ ,

H(x) = 1 when x > 0,

 $D_0$  = molecular diffusion coefficient.

The reciproke of the left-hand side of equation (3) is referred to as MacMullin number (Kyi and Batchelor, 1994) and only depends on the structure of the cement matrix, whereas H is the Heaviside function. The value of 0.18 is called the percolation threshold (Bentz and Garboczi, 1992). Equation (3) holds for a standard unleached cement matrix. During leaching, however, CH in the sample is dissolved, resulting in extra porosity. The total porosity in a leached sample  $\varphi_{\rm t}$  therefore exists of both initial (or water) porosity  $\varphi_{\rm w}$ , and a porosity fraction originating from the CH fraction  $\varphi_{\rm CH}$  that was present before leaching:

$$\varphi_{t} = \varphi_{w} + \varphi_{Ctt'} \tag{4}$$

where

 $\varphi_t$  = total porosity (= porosity after leaching)

 $\varphi_{w}$  = water porosity (= porosity before leaching),

Unfortunately, equation (3) does not hold during leaching because the diffusivity increases much more rapidly during leaching compared to the decrease in diffusivity during hydration (Bentz and Garboczi, 1992; Snyder and Clifton, 1995). This means that for a certain porosity the diffusivity in a leached sample is higher than in the unleached form and cannot be derived by simply substituting  $\varphi_i$  into equation (3). Snyder and Clifton (1995) developed equations that take this effect into account. They defined the following functions  $\varphi_w$  and  $\varphi_t$  as the results of substituting  $\varphi_w$  and  $\varphi_t$  respectively into equation (3)::

$$\vartheta_{\rm w} = 0.001 + 0.07 \,\varphi_{\rm w}^2 + H(\varphi_{\rm w} - 0.18) \cdot 1.8 \cdot (\varphi_{\rm w} - 0.18)^2 \tag{5}$$

$$\vartheta_{t} = 0.001 + 0.07 \, \varphi_{t}^{2} + H(\varphi_{t} - 0.16) \cdot 1.8 \cdot (\varphi_{t} - 0.16)^{2}$$
(6)

Using these expressions the relative diffusion coefficient in a leached sample was calculated as follows::

$$\frac{D_{\rm e}}{D_{\rm o}} = 2\,\vartheta_{\rm t} - \vartheta_{\rm w} \tag{7}$$

As indicated by equation (6), during leaching a percolation threshold of 0.16 is used instead of 0.18 (Bentz and Garboczi, 1992). Therefore this value should be used for calculating  $\vartheta_t$  for a leached sample while 0.18 is appropriate for calculating  $\vartheta_w$  of the original sample. Using these two different percolation thresholds the relative diffusion coefficient can now be calculated according to equation (7). The first term of the final equation however should be a cut-off value in case both  $\varphi_w$  and  $\varphi_t$  tend

to zero. A value of 0.001 is considered an appropriate mean value for samples that contain a certain amount of CH. However, in a leached shell that consists purely of CSH and does not contain CH anymore, a cut-off value of 0.0025 should be used, which is the relative diffusion coefficient for the CSH phase. Combining all equations now yields:

$$\frac{D_{\rm e}}{D_0} = 0.0025 + 0.07\,\varphi_{\rm w}^2 + H(\varphi_{\rm w} - 0.18) \cdot 1.8 \cdot (\varphi_{\rm w} - 0.18)^2 
+ 0.14\,\varphi_{\rm t}^2 + H(\varphi_{\rm t} - 0.16) \cdot 3.6 \cdot (\varphi_{\rm t} - 0.16)^2$$
(8)

As can be concluded from the previous analysis, the (CH fraction has two opposite effects on the metal release rate during acid attack, namely:

- 1. A positive effect by increasing acid buffering capacity,
- A negative effect by increasing porosity in the leached shell, thereby increasing the effective diffusion coefficient.

This means that the cement composition can be optimized by varying this variable in order to obtain an optimal resistance against acid attack. To this end, using equations (2) and (8), equation (1) is rewritten as:

$$\frac{M(t)}{\sqrt{2 \cdot C_0^2 \cdot f_{\text{mo}}^2 \cdot C_{\text{H}} \cdot D_0}} = f(\varphi_{\text{CH}}, \varphi_{\text{w}}, \varphi_{\text{CSH}}) =$$

$$\sqrt{\frac{0.025 - 0.07 \,\varphi_{\text{w}}^2 - H(\varphi_{\text{w}} - 0.18) \cdot 1.8 \cdot (\varphi_{\text{w}} - 0.18)^2 + 0.14 \,\varphi_{\text{t}}^2 + H(\varphi_{\text{t}} - 0.16) \cdot 3.6 \cdot (\varphi_{\text{t}} - 0.16)^2}{60.4 \cdot \varphi_{\text{CH}} + 16.5 \cdot \varphi_{\text{CSH}}}}$$
(9)

Note that the right-hand side solely depends on the cement composition, while the left-hand side contains all contaminant properties.

The cement hydration model of Bentz and Garboczi (1992), is based on the hydration of  $C_3S$  only and the corresponding volume stoichiometries of this reaction as determined by Young and Hansen (1987). Many studies revealed this hydration to be representative for the hydration of OPC (Ordinary Portland Cement). In terms of volumes  $C_3S$  reacts as follows:

$$C_3S --> 1.7 \text{ CSH} + 0.61 \text{ CH}$$
 (10)

Considering this simplified model and assuming that no silica is present the amounts of CSH and CH can be directly related to each other as follows:

$$\varphi_{\text{CSH}} = 2.8 \cdot \varphi_{\text{CH}} \tag{11}$$

and equation (2) then becomes:

$$\beta = 106.6 \, \varphi_{\text{CH}} \left\lceil \frac{mol}{l} \right\rceil \tag{12}$$

Inserting equation (11) into equation (9), one obtains a function  $f(\varphi_{_{\text{CH'}}}\varphi_{_{\text{W}}})$  that describes leaching rate:

$$\frac{M(t)}{\sqrt{2 \cdot C_0^2 \cdot f_{\text{mo}}^2 \cdot C_{\text{H}} \cdot D_0}} = f(\varphi_{\text{CH}}, \varphi_{\text{w}}) =$$

$$\sqrt{0.025 - 0.07 \varphi_{\text{w}}^2 - H(\varphi_{\text{w}} - 0.18) \cdot 1.8 \cdot (\varphi_{\text{w}} - 0.18)^2 + 0.14 \varphi_{\text{t}}^2 + H(\varphi_{\text{t}} - 0.16) \cdot 3.6 \cdot (\varphi_{\text{t}} - 0.16)^2}$$

$$\frac{106.6 \cdot \varphi_{\text{CH}}}{106.6 \cdot \varphi_{\text{CH}}} = \frac{1}{106.6 \cdot \varphi_{\text{CH}}} + \frac$$

In Figure 1 this function  $f(\phi_{\text{cH}},\phi_{\text{w}})$  is drawn versus (CH for various values of  $\phi_{\text{w}}$ .

One can see from Figure 1 that for each  $\varphi_W$ , a  $\varphi_{CH}$  exists for which  $f(\varphi_{CH}, \varphi_W)$  is minimal. Figure 1 also shows that the positive dependency on  $\varphi_{CH}$  of the function f is more pronounced at low water porosities, and the negative dependency on  $\varphi_{CH}$  is more pronounced at high water porosities. As expected, for every  $\varphi_{CH}$  f is lowest when  $\varphi_W$  is lowest.

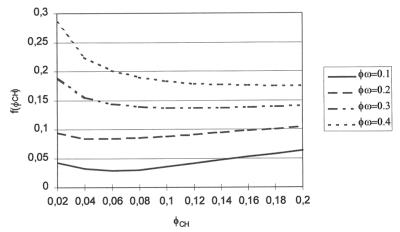


Fig. 1.  $f(\varphi_{CH})$  plotted for various water porosity fractions  $\varphi_w$ .

The  $\varphi_{\text{CH}}$  for which  $f(\varphi_{\text{CH}}, \varphi_{\text{w}})$  is minimal, denoted as  $\varphi_{\text{CH min}}$ , follows from differentiating the right-hand side of equation (13) with respect to  $\varphi_{\text{CH}}$ :

$$\frac{df(\varphi_{\rm CH}, \varphi_{\rm w})}{d\varphi_{\rm CH}} = \frac{1}{2f} \cdot \frac{0.14\varphi_{\rm CH}^2 + H(\varphi_{\rm w} - 0.18) \cdot 1.8 \cdot (\varphi_{\rm w} - 0.18)^2 - 0.0025 - 0.07 \varphi_{\rm w}^2}{\varphi_{\rm CH}^2} + \frac{1}{2f} \cdot \frac{H(\varphi_{\rm t} - 0.16) \cdot 3.6 \cdot (\varphi_{\rm CH}^2 - \varphi_{\rm w}^2 + 0.32 \varphi_{\rm w} - (0.16)^2)}{\varphi_{\rm CH}^2}$$
(14)

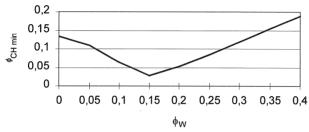
Setting the right-hand side equal to zero yields::

$$\varphi_{\text{CH}} = \sqrt{0.5\,\varphi_{\text{w}}^2 + 0.0178}$$
 for  $\varphi_{\text{w}} < 0.16, \, \varphi_{\text{t}} < 0.16$  (15)

$$\varphi_{\text{CH}} = \sqrt{0.98\,\varphi_{\text{w}}^2 - 0.308\,\varphi_{\text{w}} + 0.025}$$
 for  $\varphi_{\text{w}} < 0.18,\,\varphi_{\text{t}} > 0.16$  (16)

$$\varphi_{\text{CH}} = \sqrt{0.5\,\varphi_{\text{w}}^2 - 0.135\,\varphi_{\text{w}} + 0.0097} \qquad \text{for} \qquad \varphi_{\text{w}} > 0.18, \, \varphi_{\text{t}} > 0.16$$
 (17)

In Figure 2a this  $\varphi_{\text{CH min}}$  is plotted for different values of  $\varphi_{\text{w}}$ . In Figure 2b the corresponding  $f(\varphi_{\text{t}})$  minima, denoted as  $f_{\min}$  are plotted versus  $\varphi_{\text{w}}$ .



*Fig. 2a.* For which  $f(\varphi_i)$  is minimal  $(\varphi_{CH min})$  plotted for various values of  $\varphi_m$ .

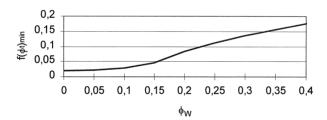


Fig. 2b. Minimum  $f(\varphi_i)$  plotted against  $\varphi_{in}$ .

The shape of Figure 2a again shows the dual effect of  $\varphi_{\text{cH}}$ . At high water porosity, when water porosity increases,  $\varphi_{\text{cH}}$  must also increase in order to keep f minimal. At low water porosity however,  $\varphi_{\text{CH}}$  must decrease as in that case  $\varphi_{\text{CH}}$  also has an increasing effect on f. From Figure 2b the major effect of  $\varphi_{\text{w}}$  on  $f_{\text{min}}$  is illustrated. From Figure 2a and 2b one can conclude that  $f(\varphi_{\text{CH}}, \varphi_{\text{w}})$  is lowest if  $\varphi_{\text{w}}$  equals zero and  $\varphi_{\text{CH}}$  is about 0.13.

## 3 Calculation of optimal w/c ratio

In the previous section  $\varphi_{\text{cH}}$  and  $\varphi_{\text{w}}$  have been treated as independent variables. These properties can, however, be related using the hydration equation used by Bentz and Garboczi (1992), which was given in equation (10) and their typical specific gravity of 3200 kg/m³ for cement. Using this information from their model, the  $\varphi_{\text{cH}}$  and  $\varphi_{\text{w}}$  can be described as a function of the degree of hydration ( $\alpha$ ) and water/cement ratio (w/c) as follows:

$$\varphi_{\rm CH} = \frac{0.191 \,\alpha}{w/c + 0.313},\tag{18}$$

$$\varphi_{\rm w} = \frac{w/c - 0.410 \,\alpha}{w/c + 0.313},\tag{19}$$

and hence,

$$\varphi_{\rm t} = \varphi_{\rm CH} + \varphi_{\rm w} = \frac{w/c - 0.219 \,\alpha}{w/c + 0.313},\tag{20}$$

where:

 $\varphi_t$  = total porosity fraction,

 $\varphi_{CH} = Ca(OH)_2$  fraction,

 $\varphi_{w}$  = water porosity fraction,

w/c = water/cement ratio,

 $\alpha$  = hydration degree.

Both fractions  $\varphi_{cu}$  and  $\varphi_{w}$  can be substituted into equation (13), yielding f as a function of w/c and  $\alpha$ . In Figure 3 f(w/c) is depicted for various  $\alpha$ , namely  $\alpha = 0.30, 0.60, 0.90$  and 1. Considering that  $\alpha < w/c$  ratio / 0.41, for every w/c ratio < 0.41 hydration cannot be attained completely ( $\alpha = 1$ ). Hence, in this case there is a maximum achievable  $\alpha$ , depicted as  $\alpha_{max}$ . For w/c > 0.41, hydration can proceed until  $\alpha_{max}$  = 1. The function  $f(\alpha_{max})$  is also drawn in Figure 3. As both time and hydration proceed, for each w/c ratio the function f decreases till the lines corresponding to  $\alpha_{max}$  or  $\alpha = 1$  are attained. One can readily see that for practical purposes w/c ratio should be as low as possible. At low w/c ratio however, the differences in lowest achievable f values are very small with f ranging from about 0.025 to 0.05 for w/c ratio ranging from 0.2 to 0.41, respectively. Therefore, using a w/cratio < 0.41 will be of no use in practice as it does not result in a substantial decrease in f anymore. Moreover, unhydrated cement will then remain, being unused for binding and immobilization. In Figure 4  $f(\alpha)$  is depicted for various w/c ratio, namely w/c = 0.3, 0.4, 0.5 and 0.6 for  $\alpha = 0$  till  $\alpha$  =  $\alpha_{max}$ . From this figure it is clear that f decreases during hydration. One may also conclude from Figure 4 that using a higher w/c ratio can only result in a lower f value when hydration degree is significantly higher. At complete hydration a higher w/c ratio will always result in a higher leaching rate.

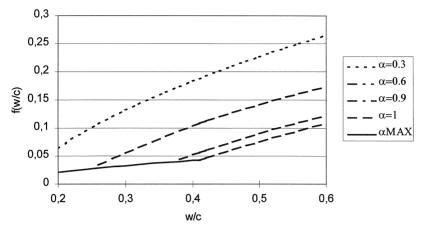


Fig. 3. f(wcf) plotted against w/c for various  $\alpha$ .

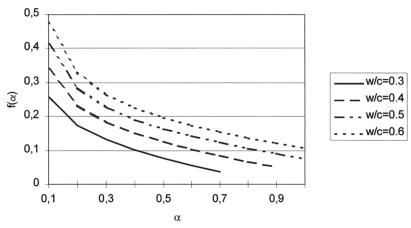


Fig. 4.  $f(\alpha)$  plotted against  $\alpha$  for various w/c.

# 4 Comparison with experiments

In the previous section a theoretical model has been presented for the leaching from hydrated cement matrices. In this section the theoretical predictions are compared with some experimental data obtained from the literature.

Zamorani and Serrini (1992) performed leaching experiments on  $Cs^+$ -ions immobilized in cement samples at different w/c values. Ordinary Portland cement was used and all samples were cured at 60 °C, 98% R.H. for 11 days. The samples were leached in water at a surface-to-liquid volume of 0.1/cm. It was found that the cumulative fraction leached (CFR) depends on both  $\sqrt{t}$ , which is in qualitative agreement with equation (1) and the w/c ratio.  $C_0$ ,  $f_{\rm mor}$   $C_{\rm H}$  and  $D_0$  can be assumed con-

stant for each of their experiments and were calibrated using their results for w/c = 0.4. The CFR can now be related to f via:,

$$\frac{CFR}{CFR_{\text{wcf}=0.4}} = \frac{f}{f(w/c=0.4)} \tag{21}$$

Densities and total pore volumes of all samples are given by the reference in [g/cm³] and [cm³/g], respectively. In order to obtain the water porosity fractions  $\varphi_w$  for each sample the given total pore volumes in [cm³/g] were multiplied with the measured and reported sample densities. These resulting water porosity fractions were then used to estimate the hydration degree  $\alpha$  of every sample using the relation between these two as given in equation (19). Using this estimated hydration degree  $\alpha$ , f was calculated for each w/c ratio used in the experiments.

In Table I the calculated f ratios are compared with CFR ratios for various w/c ratio. One can readily conclude that the agreement between experiments and the here presented model predictions are good, especially when one considers the simplifications invoked in the present analysis. This 'implies that the combination of leaching model and cement composition, resulting in the

This 'implies that the combination of leaching model and cement composition, resulting in the function *f*, well describes the leaching process as a function of cement composition.

Table 1.	f ratios comp	paerd to CFR ratio	s (Zamorano and Serri	ine, 1992).
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wcf	estimated $\alpha$	$CFR/CFR_{W/c=0.4}$	f/f(w/c=0.4)
0.35	0.49	0.89	0.89
0.4	0.53	1	1
0.45	0.52	1.24	1.19
0.5	0.65	1.36	1.25

## 5 Addition of silica fume

Silica fume, a highly reactive amorphous silica material, can be used as an admixture. It reacts with the CH released during hydration and forms CSH. Two situations should be considered when silica (in cement chemistry notation: *S*) is present:

1. All CH produced during hydration of the cement is consumed by the initial amount of S, forming CSH. This implies that some unreacted silica remains in the hydrated sample, while  $\varphi_{\text{CH}} = 0$ . The relevant volume fractions can be calculated as follows (Bentz and Garboczi, 1992):,

$$\varphi_{w} = 1 - \frac{(1+1.755a)(1-m) + 1.45m}{3.2 \cdot (w/s + 0.14m) + 1},$$
(22)

$$\varphi_{\text{CSH}} = \frac{3.048 \,\alpha (1 - m)}{3.2 \cdot (w/s + 0.14m) + 1},\tag{23}$$

$$\varphi_{\rm S} = \frac{1.45m - 0.293 \,\alpha(1 - m)}{3.2 \cdot (w/s + 0.14m) + 1},\tag{24}$$

where

w/s = water/solid ratio (i.e. cement and silica fume)

m = silica fume mass/cement and silica fume mass

 $\varphi_{S} = S$  volume fraction

By definition the w/s ratio and the w/c ratio can be related to each other as follows:

$$w/s = (1 - m) \cdot w/c \tag{25}$$

The corresponding silica fume volume fraction x can be related to the mass fraction m as follows (Bentz and Garboczi, 1992):

$$x = \frac{3.2m}{2.2(1-m) + 3.2m} \tag{26}$$

2. More CH is produced during hydration than can be consumed by the initial amount of *S*. This situation occurs when the amount of CH produced is higher than the amount of CH consumed, which means that (Bentz and Garboczi, 1992):

$$0.61(1-x)\alpha > 2.08x\tag{27}$$

or

$$m \le \frac{\alpha}{\alpha + 4.96} \tag{28}$$

where 0.61 is the amount of CH produced by one volume element of  $C_3S$  and 2.08 is the amount of CH consumed by one volume element of S.

When the silica fume fraction fulfills condition (27) a CH fraction will remain in the final sample and all volume fractions of interest can be calculated as follows (Bentz and Garboczi, 1992):

$$\varphi_{\text{CSH}} = \frac{1.7\,\alpha(1-m) + 6.67m}{3.2\cdot(w/s + 0.14m) + 1},\tag{29}$$

$$\varphi_{\text{CH}} = \frac{0.61 \alpha (1 - m) - 3m}{3.2 \cdot (w/s + 0.14m) + 1},\tag{30}$$

and

$$\varphi_{\rm w} = 1 - \frac{2.3 \alpha (1 - m) + (1 - \alpha) + 3.67m}{3.2 \cdot (w/s + 0.14m) + 1},\tag{31}$$

In the presence of silica fume the amounts of CSH and CH are no longer related by equation (11). Therefore the simplified equation (12) for the ANC is not valid anymore and equation (2) should be used instead, in which  $\varphi_{\text{CSH}}$  and  $\varphi_{\text{CH}}$  are calculated separately in order to obtain the ANC. Using the f function from equation (9) and equations (29)-(31) for all volume fractions, f(m) can be calculated for samples with silica fume. In Figure 5 the function f(m) is plotted for various w/s, namely 0.35, 0.40, 0.5.  $\alpha$  was taken as 0.7, which means that, according to equation (27), when m > 0.12,  $\varphi_{\text{CH}} = 0$  and silica remains in the sample.

The amount of S is optimal when f is as low as possible, but it should be noted that also S as such should be as low as possible, considering its high price. From Figure 5 it can be seen that such optima exist. Silica replaces CH with CSH in a sample. Because calcium is more strongly bound in CSH compared to CH this calcium contributes less to the ANC (see also equation (2)). In other words, the replacement of CH for CSH makes the calcium less available for buffering. As from the point where all CH is consumed, the addition of more silica still has a negative effect on the ANC because then it replaces cement and less CSH is formed during hydration. Low amounts of silica have a negative effect on total porosity during the leaching process, because less CH is leached out. However at the point where silica remains, higher amounts of silica only acts as inert filler, replacing the initial amount of cement and increasing the final water porosity. These effects are responsible for the shape of the plots in Figure 5. The minima in these plots correspond to the point where all CH is consumed because at that point both water- and total porosities are minimal. This optimum can therefore be determined straightforward using equation (28). In this case, when  $\alpha = 0.7$ , the silica fume mass fraction where f(m) is minimal is m = 0.12. From Figure 5 one can also see that for w/s < 0.5 adding more than 8 mass % silica fume is not very useful anymore.

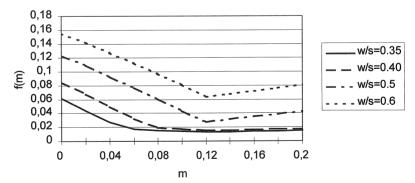


Fig. 5. f(m) plotted against silica fume mass fraction m for various w/c ( $\alpha = 0.7$ ).

In Figure 6 f(m) is plotted for various  $\alpha$ . The w/s was taken as 0.4. As can be seen from Figure 6 low f(m) values are only possible at high hydration rates and the minima are different for all considered

 $\alpha$ . The line  $\alpha$  = 0.9 ends at 8 mass % silica fume because this hydration degree is not achievable anymore for samples that contain more silica fume.

From both figures it can be concluded that in general, for all w/s and  $\alpha$  values used here, optimal silica fume contents vary between 8 and 10 mass % when ( ranges from 0.3 to 0.6, respectively. For low w/s or high hydration degrees the addition of 8 mass % silica fume would be the most appropriate in theory.

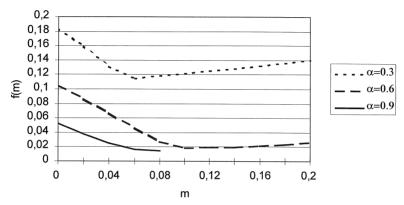


Fig. 6. f(x) plotted against silica fume mass fraction m for various w/c ( $\alpha = 0.4$ ).

## 6 Conclusions

By combining the shrinking core leaching model and equations for the effective diffusion coefficient leaching rates can be determined as function of cement composition. When the water porosity fraction is known a CH fraction can be calculated at which leaching rates are minimal. Because the water porosity only has a negative effect, it should always be as low as possible. Cement composition should therefore be optimized for the amount of CH. Best results are obtained when water porosity is 0 % and CH fraction is 13 %.

Leaching rates can also be determined as function of the w/c ratio. From this it follows that minimal leaching rates can only be obtained at very low w/c ratio. In order to use all cement, additions such as silica fume are needed. The optimal relative amount of silica fume mostly depends on the expected hydration degree  $\alpha$  and less on the w/c ratio used. Optimal values were determined, which varied between 8-10 mass % based on total mass of cement and silica fume.

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